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Antiferro- and ferromagnetic ordering in a PrGe single crystal

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Abstract

An equiatomic PrGe single crystal was grown by the Czochralski pulling method. The grown single crystal was found to have CrB-type orthorhombic crystal structure with the space group Cmcm (no. 63). Transport and magnetization data reveal large anisotropy in the electrical resistivity, magnetic susceptibility and magnetization. PrGe was found to exhibit two consecutive magnetic orderings at 44 K and 41.5 K, respectively. The magnetic susceptibility measurement along the three principal directions in low applied fields revealed a cusp-like behaviour at 44 K while at 41.5 K a ferromagnetic-like increase was observed. The hysteretic behaviour in the magnetization measurement at 1.8 K confirmed the ferromagnetic nature of PrGe at low temperatures. The heat capacity data clearly revealed the bulk nature of two magnetic transitions by the presence of two sharp peaks attaining values exceeding $40 \text{ J K}^{-1} \text{ mol}^{-1}$ at the respective temperatures. The absence of a Schottky contribution in the magnetic part of the heat capacity indicates a quasi-ninefold degenerate J=4 magnetic ground state in this system. The low temperature data of electrical resistivity and the magnetic part of the heat capacity show the existence of a gap in the spin-wave spectrum.

(Some figures may appear in colour only in the online journal)

1. Introduction

The equiatomic RX series of compounds with R as rare earth and X as either Si, Ge, Ni or Pt, crystallizing in the orthorhombic crystal structure, exhibits not only interesting structural properties but also interesting magnetic properties [1-3]. One of the earliest structural studies on this RX (R = rare earth, X = Si, Ge, Ni, Pt) was performed by Hohnke and Parthé [4] about five decades ago. They found that RSi (R = La-Er) crystallize in the FeB-type structure while the higher rare earths from Dy to Er in this series exhibit polymorphic behaviour by crystallizing in CrB-type orthorhombic structure as well. On the other hand, most of the RGe compounds (R = Nd-Er) crystallize in the CrB-type crystal structure. The RGe compounds of lighter rare earths, namely La and Ce, crystallize in the FeB-type structure, while PrGe exhibits polymorphism by crystallizing in the FeB- and CrB-type orthorhombic crystal structures,

depending on the preparation conditions. Buschow and Fast [5] investigated the magnetic properties of polycrystalline samples of RGe (R = La-Er) and reported that PrGe and NdGe order ferromagnetically, while CeGe, SmGe, GdGe, TbGe, DyGe, HoGe and ErGe exhibit antiferromagnetic ordering on cooling. In EuGe, the Eu was found to have divalent nature with an antiferromagnetic ordering at 20 K [6]. From neutron diffraction study, Schobinger-Papamantellos and Buschow [7] have confirmed the ferromagnetic ordering in NdGe with a Curie temperature of 28 K. Furthermore, they stabilized PrGe in its two polymorphic forms and reported a T_C of 36 K for FeB-type and 39 K for CrB-type orthorhombic structure with the magnetic moment pointing along the c-axis. Lambert-Andron et al [8] have investigated the off-stoichiometric PrGe_{1.66} compound, which was found to exist in two different crystallographic structures possessing the ordered and disordered variants of the ThSi₂-type crystal structure. They reported that the both the ordered and disordered phases are ferromagnetic, with ordering temperatures at 19 and 14 K respectively. Recently, we investigated the anisotropic magnetic properties of CeGe single crystal in detail, which orders antiferromagnetically with a Néel temperature of 10.5 K [9]. The magnetic easy axis was found to be along the [010] direction. The electrical resistivity of CeGe showed an upturn at the Néel temperature, indicating the superzone gap formation. In continuation of our studies on RGe compounds, and as there are no further detailed studies on the PrGe compound, we have grown a single crystal of PrGe and report the anisotropic magnetic properties here.

2. Experiment

The binary phase diagram of PrGe revealed that PrGe melts congruently [10] at 1400 °C, hence we adopted the Czochralski crystal pulling method to grow the single crystal in a tetra-arc furnace. The starting materials were high purity metals of Pr (99.95%) and Ge (99.999%). A total of 10 g of the stoichiometric PrGe was repeatedly melted several times to make a homogeneous mixture. A thin polycrystalline seed rod was cut out of this polycrystalline material and immersed into the melt and pulled at a speed of 10 mm h⁻¹ in a pure and dry argon atmosphere. The crystal was pulled for about 6-7 h to obtain a 70 mm long crystal with a diameter of roughly 3-4 mm. The phase purity of the single crystal was investigated by means of powder x-ray diffraction using a PANalytical machine. The single crystal was oriented along the principal crystallographic directions by means of Laue back reflection using a Huber Laue diffractometer and cut to the desired dimensions using a spark erosion cutting machine. For the non-magnetic reference compound, a polycrystalline sample of YGe was prepared by melting stoichiometric amounts of high purity Y and Ge in an arc-melting furnace. The polycrystalline sample was then annealed at 1100 °C for one week in a resistive heating furnace. The magnetic measurements were performed using a quantum interference device (SQUID) magnetometer and vibrating sample magnetometer (VSM). The electrical resistivity measurement was performed in a home-made resistivity set-up in the temperature range from 1.8 to 300 K. The heat capacity measurement was performed using a physical property measurement system (PPMS).

3. Results

3.1. X-ray diffraction

Owing to the fact that PrGe exists in two polymorphic forms [7], namely the CrB- and FeB-type orthorhombic crystal structures with the space groups Cmcm (#63) and Pnma (#62) respectively, as a first step we wanted to confirm the phase purity and the crystal structure of our single crystal. A small portion of the grown crystal was subjected to powder x-ray diffraction at 300 K using monochromatic Cu K α radiation with the wavelength 1.5406 Å. The x-ray pattern reveals that the grown crystal possesses the CrB-type structure

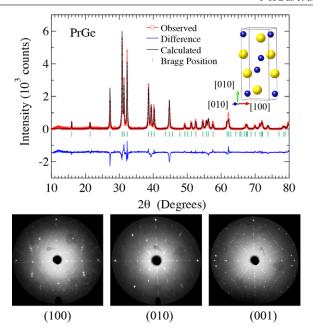


Figure 1. Powder x-ray diffraction pattern of PrGe together with the Rietveld refinement pattern. The inset shows the crystal structure of PrGe. The Laue diffraction patterns corresponding to (100), (010) and (001) are also shown.

as the major phase (figure 1). A Rietveld refinement using the Fullprof program [11] confirmed the orthorhombic crystal structure of CrB type with the space group Cmcm. The lattice constants were estimated to be $a = 4.4808(\pm 0.5066 \times 10^{-3})$, $b = 11.087(\pm 0.1101 \times 10^{-2})$ and $c = 4.050(\pm 0.3855 \times 10^{-2})$ 10^{-3}) Å with the reliability parameters $R_{\rm B} = 12.4\%$ and $R_{\rm F} = 6.50\%$. The lattice constants are in close agreement with those reported in [7]. Both the Pr and Ge atoms occupy the 4c Wyckoff position, with y = 0.3608(3) and 0.0785(5), respectively. The stoichiometry of the grown crystal was further confirmed by means of energy dispersive analysis by x-ray measurement. The back reflection Laue pattern of the grown crystal was characterized by well defined Laue diffraction spots, ascertaining the high quality of the crystal, and it was also employed to identify the three principal crystallographic directions as shown in figure 1. The crystal was then cut along the principal directions by means of the spark erosion cutting machine for the anisotropic physical property measurements.

3.2. Magnetic susceptibility and magnetization

Figure 2(a) shows the temperature dependence of magnetic susceptibility of PrGe measured in an applied magnetic field of 0.1 T in the temperature range from 1.8 to 300 K for $H \parallel [100]$ and [010] directions. There is a large anisotropy in the magnetic susceptibility along the two directions. Signatures of two magnetic orderings at 44 K and at 41.5 K are observed along both [100] and [010] directions. From the inset of figure 2(a) it is obvious that the high temperature ordering at 44 K indicates a cusp-like behaviour usually observed in the case of antiferromagnetic ordering. At 41.5 K

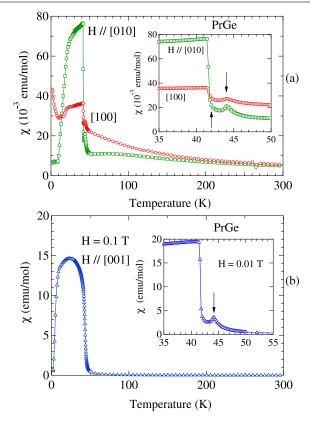


Figure 2. (a) Temperature dependence of magnetic susceptibility of PrGe along [100] and [010] directions, measured in an applied field of 0.1 T. (b) Susceptibility of PrGe along the [001] direction measured in an applied field of 0.1 T. The insets in both parts show the expanded scale susceptibility near the ordering temperature. The arrows indicate the magnetic ordering. The inset in (b) shows data measured in a field of 0.01 T.

the magnetic susceptibility shows an upturn signalling a ferromagnetic ordering. For $H \parallel [100]$, below 10 K, the susceptibility increases: this may be attributed to the canting of the ordered Pr moments along this hard axis and/or to crystallographic defects. The magnetic susceptibility for $H \parallel$ [001] is shown in figure 2(b). Unlike the other two directions, the susceptibility in a field of 0.1 T apparently exhibits only one ordering at 44 K, which is ferromagnetic-like. However, when the data are recorded in a lower field of 0.01 T (inset of figure 2(b)) the antiferromagnetic ordering at 44 K is clearly observed in the [001] direction as well, followed by a ferromagnetic-like upturn at lower temperatures. The in-field, isothermal magnetization data to be discussed later further substantiate this claim. The inverse magnetic susceptibility of PrGe is shown in figure 3. The anisotropy in the magnetic susceptibility along the three principal directions is clearly evident. The solid lines are fits to the modified Curie-Weiss law $\chi = \chi_0 + C/(T - \theta_p)$. It is observed that the Curie-Weiss law is obeyed from 300 K to immediately above the magnetic ordering and no deviation due to the crystal electric field effect is observed. From the fitting, the effective magnetic moment μ_{eff} , the paramagnetic Curie temperature θ_p and the temperature independent magnetic susceptibility χ_0 were found to be 3.78 μ_B , -24 K and 6.794 \times 10⁻⁵ emu mol⁻¹; 3.90 μ_B , -70 K and 1.8166 \times

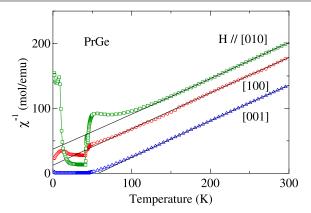


Figure 3. Inverse magnetic susceptibility of PrGe along the three principal crystallographic directions; the solid lines are fits to the modified Curie–Weiss law.

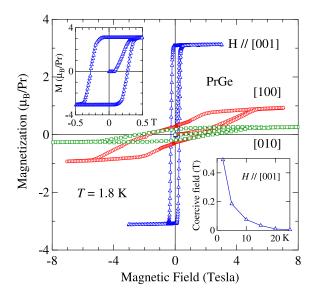


Figure 4. Isothermal magnetization of PrGe measured at temperature 1.8 K for fields along the three principal crystallographic directions. The upper inset shows the low field part of the hysteresis loop for $H \parallel [001]$. The lower inset shows the temperature dependence of the coercive field for $H \parallel [001]$.

 10^{-4} emu mol $^{-1}$ and 3.71 $\mu_{\rm B}$, 58 K and 2.5831 \times 10^{-4} emu mol $^{-1}$, respectively, for $H \parallel$ [100], [010] and [001]. The experimental value of the effective moment $\mu_{\rm eff}$ is close to the free ion value of Pr^{3+} , 3.58 μ_B . The Weiss temperature $\theta_{\rm D}$ is positive for $H \parallel [001]$, as expected for a ferromagnetic ordering compound. On the other hand, θ_p is negative for $H \parallel$ [100] and [010] due to the antiferromagnetic ordering at 44 K. The isothermal magnetization of PrGe measured at T = 1.8 Kalong the three principal crystallographic directions is shown in figure 4. Hysteretic behaviour is observed along all the three directions, confirming the ferromagnetic ground state in PrGe, thus corroborating the previous neutron diffraction results on a polycrystalline sample of PrGe [7]. For $H \parallel [001]$ the magnetization increases more rapidly with field than along the other two directions, thus indicating the [001] direction as the easy axis of magnetization. At 1.8 K the magnetization saturates to 3.12 μ_B/Pr , very close to the saturation moment

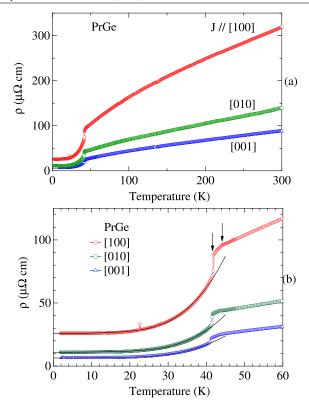


Figure 5. (a) Temperature dependence of electrical resistivity of PrGe for current parallel to the three principal crystallographic directions. (b) The low temperature part of the resistivity of PrGe. The solid lines are the fit to the spin-wave gap model given in equation (1).

of the free Pr^{3+} ion $(g_J J \mu_B = 3.20 \mu_B)$. The saturation values of the magnetic moment along the [100] and [010] directions are much smaller, indicating the hard axes of magnetization. The width of the hysteresis loop decreases as the temperature increases, and above 42 K, where the sample enters the antiferromagnetic state, there is no signature of hysteresis. This is shown in the lower inset of figure 4 as a plot of coercive field versus temperature for $H \parallel [001]$. For $H \parallel [001]$ the slope of the virgin curve is small, which indicates the presence of narrow domain walls [12]. The impurities of atomic dimensions pin the domain wall, as is evident from the flat virgin curve up to a field of 0.08 T (see the inset of figure 4), at which point the magnetization increases, which means the external field is able to detach the pinned domain wall at this field of 0.08 T; the complete detaching of the pinned domain wall occurs at 0.4 T and at higher fields the domain walls are completely removed. On reversing the field the reversed domain walls nucleate, and only for negative fields of about 0.4 T are the domain walls removed.

3.3. Electrical resistivity

Figure 5(a) shows the temperature dependence of electrical resistivity of the PrGe single crystal measured for current parallel to [100], [010] and [001]. The electrical resistivity decreases with decreasing temperature along the three

Table 1. Fitting parameters of the resistivity data along the three principal directions described in equation (1).

	$\rho_0 (\mu \Omega \mathrm{cm})$	$a (\mu \Omega \mathrm{cm} \mathrm{K}^{-2})$	$D~(\mu\Omega~{\rm cm}~{\rm K}^{-2})$	Δ (K)
ρ _[100]	26	0.004	0.14	150
$\rho_{[010]}$	10	0.002	0.07	154
$\rho_{[001]}$	6.4	0.001	0.03	142

directions and the magnetic ordering is clearly visible from the sharp drop due to the reduction in the spin-disorder scattering. There is a large anisotropy in the electrical resistivity, with room temperature values of $\rho_{[100]}(300 \text{ K}) =$ 319 $\mu\Omega$ cm, $\rho_{[010]}(300 \text{ K}) = 139 \,\mu\Omega$ cm and $\rho_{[001]}(300 \text{ K}) =$ 88 $\mu\Omega$ cm for PrGe. Figure 5(b) shows the low temperature part of the electrical resistivity. The high temperature antiferromagnetic ordering T_N is observed at 44 K by a very small change of slope. The ferromagnetic ordering $T_{\rm C}$ at 41.4 K shows a sharp drop in the electrical resistivity along all three directions. At T_N there is a decrease in the resistivity. However, just immediately below this temperature, the Pr moments again re-orient themselves to the ferromagnetic ordering; because of this, the resistivity drop is not so prominent between T_N and T_C . Once the ferromagnetic ordering sets in, the electrical resistivity drops more rapidly due to the reduction in the spin-disorder scattering. This type of sharp drop in the electrical resistivity is attributed to the first order transition. The electrical resistivity of PrGe in the ferromagnetically ordered state can be fitted to the expression

$$\rho(T) = \rho_0 + aT^2 + DT\Delta \left(1 + \frac{2T}{\Delta}\right) \exp\left(-\frac{\Delta}{T}\right), \quad (1)$$

which involves, apart from the usual Fermi liquid term, the contribution from the energy gap in the magnon dispersion relation [13]. In equation (1), ρ_0 is the residual resistivity, a is the coefficient responsible for electron–electron scattering, D is the coefficient of electron–magnon scattering and Δ is the magnitude of the spin-wave gap. The low temperature part of the electrical resistivity is very well explained by the above expression up to 40 K, as seen by the solid lines in figure 5(b). The parameters obtained from the fit are given in table 1.

The obtained values of the spin-wave gap are nearly equal for all three directions, even though there is a large anisotropy in the electrical resistivity. The residual resistivity ratio (RRR) amounts to 12.22, 12.52 and 13.54 for $J \parallel [100]$, [010] and [001] respectively, thus indicating good quality of the single crystal.

3.4. Heat capacity

The temperature dependence of the specific heat of the PrGe single crystal and its non-magnetic reference compound YGe measured in the range of 1.8–150 K is shown in the main panel of figure 6(a). Since the crystal structure of LaGe is FeB type, which is different from the CrB-type structure of PrGe, we have prepared a polycrystalline sample of YGe which possesses the same crystal structure as that of PrGe and used it as the non-magnetic reference compound, after

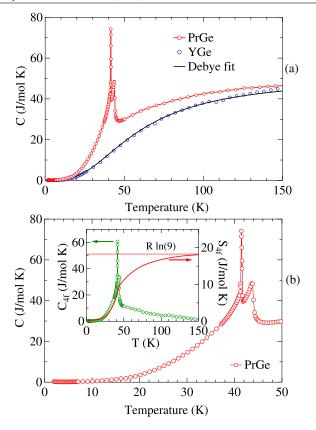


Figure 6. (a) Temperature dependence of the specific heat capacity in PrGe and YGe. The solid line through the data points of YGe is fitted to the Debye model of heat capacity. (b) The main panel shows the low temperature part of the specific heat of PrGe and the inset shows the magnetic part of the heat capacity and the calculated entropy.

taking into account the mass renormalization as mentioned in [14]. The heat capacity of YGe can be very well fitted to the Debye model as shown by the solid line through the data points of YGe, and Θ_D was estimated to be 245 K. Furthermore, an estimation of γ was made from the low temperature heat capacity data of YGe, and it was found to be 3.4 mJ K^{-2} mol⁻¹. The two magnetic orderings are observed exactly at the same temperatures as the corresponding values in the magnetic susceptibility and the resistivity data, thus confirming the two bulk magnetic orderings in PrGe. Figure 6(b) shows the low temperature part of the heat capacity of PrGe, which clearly depicts both the magnetic orderings. The jump in the heat capacity at the first magnetic ordering at 44 K amounts to 19.29 J K⁻¹ mol⁻¹, while at the second magnetic ordering, namely where the system undergoes the ferromagnetic ordering, a very sharp peak with a jump of about 45.06 J K⁻¹ mol⁻¹ is observed. This sharp jump at 41.5 K together with the sharp resistivity drop, as mentioned earlier, clearly indicates that this is a first order transition. Further confirmation for the first order nature of the ferromagnetic transition at 41.5 K comes from the shape of the Arrott plots (vide infra). An estimation of the magnetic part of the heat capacity of PrGe was obtained by subtracting the heat capacity of YGe, which is assumed as the lattice part of the heat capacity. The temperature dependence of entropy

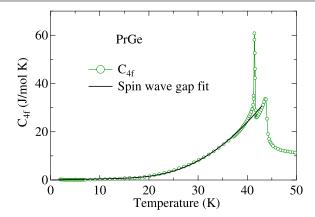


Figure 7. The magnetic part of the heat capacity (C_{4f}) ; the solid line is the fit to the spin-wave expression given in equation (2).

was obtained by integrating the C_{4f}/T data, as shown in the inset of figure 6(b). In the ferromagnetically ordered state, the magnetic contribution to the heat capacity C_{4f} of PrGe can be fitted to the spin-wave gap expression [15], which is given by

$$C_{4f} = \gamma T + C_{SW}, \tag{2}$$

where

$$C_{\text{SW}} = \alpha \left(\frac{\Delta^2}{\sqrt{T}} + 3\Delta\sqrt{T} + 5\sqrt{T^3} \right) e^{\frac{-\Delta}{T}}.$$
 (3)

Here, γ is the electronic term of the heat capacity and $C_{\rm SW}$ is the contribution to the ferromagnetic spin-wave excitation spectrum with an energy gap Δ , and α is a constant. It is evident from figure 7 that equation (2) fits very well the $C_{\rm 4f}$ data from up to 40 K. The obtained values of the fitting parameters are $\gamma=45.9$ mJ K⁻² mol⁻¹, $\alpha=0.105$ J (K^{-5/2} mol⁻¹) and $\Delta=140$ K. The spin-wave gap parameter Δ is in close agreement with the values obtained from the electrical resistivity data.

4. Discussion

The previous magnetic and neutron diffraction studies on polycrystalline samples of PrGe had revealed that PrGe orders ferromagnetically at 39 K [5, 7]. Furthermore, it was reported that PrGe exists in polymorphic forms, having CrB- and FeB-type orthorhombic crystal structure. The neutron diffraction pattern reported in [7] measured at 293 K consisted of diffraction patterns due to both CrB-type and FeB-type diffraction patterns. On the other hand, the PrGe single crystal studied here did not show any polymorphism. It is evident from figure 1 that the powder diffraction pattern of the PrGe single crystal measured at 300 K does not show any reflection due to the two different polymorphic structures and matches well with the CrB-type orthorhombic crystal structure with the space group Cmcm. Unlike the previous reports on polycrystalline samples, the transport and magnetic properties measured on the PrGe single crystal in the present work reveal two consecutive magnetic orderings at 44 K and 41.5 K, respectively, where the high temperature

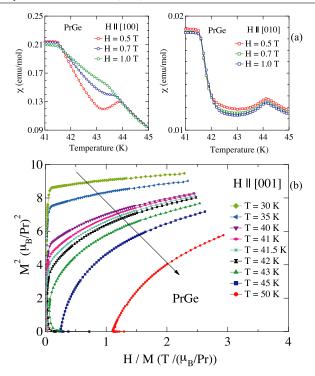


Figure 8. (a) Magnetic field dependence of the magnetic susceptibility of PrGe for $H \parallel [100]$ and [010]. (b) Arrott plots of PrGe constructed in the temperature range from 30 to 50 K; the arrow indicates the progressive increase in temperature of the plots.

ordering is antiferromagnetic in nature while the one at 41.5 K is ferromagnetic. Hysteretic behaviour is observed along all three crystallographic directions in the M versus H measurements measured at 1.8 K, thus confirming the ferromagnetic ground state of PrGe. In order to further confirm the antiferromagnetic nature of the high temperature magnetic ordering at 44 K, we performed the magnetic susceptibility measurement at various applied fields, namely 0.5, 0.7 and 1 T, as shown in figure 8. For $H \parallel [100]$, as the applied field increases the magnetic ordering temperature shifts to lower fields, typical for an antiferromagnet. When the field is applied parallel to [010], the magnetic ordering does not show any appreciable change. This can be attributed to the antiferromagnetic hard axis of magnetization. Since the magnetization along the [001] direction increases more rapidly and saturates to 3.12 μ_B/Pr , it is the easy axis of magnetization which is in conformity with the neutron diffraction result [7]. The sharp drop in the electrical resistivity and the huge jump in the heat capacity at the ferromagnetic ordering indicates a first order transition. The Arrott plots of PrGe constructed in the temperature range from 30 to 50 K are shown in figure 8(b). It is evident from the figure that the Arrott plots show an 'S' shaped curve, which is usually observed when the ferromagnetic ordering is first order [16]. It was first pointed out by Banerjee [17] that the sign of the slope of the isotherm plots M^2 versus H/M is negative for a first order ferromagnetic transition. The low temperature part of the electrical resistivity and the magnetic part of the heat capacity confirm the gap in the spin-wave spectrum. In the orthorhombic site symmetry, the

ninefold degenerate Hund's rule derived ground state ³H₄ of Pr will be split by the crystal electric field. The orthorhombic point symmetry of Pr atoms makes this degenerate level split up into nine singlets. Since PrGe orders magnetically, the low lying levels with small separation may form into an effective doublet, resulting in magnetic ordering. Just above the magnetic ordering the entropy reaches $R \ln 4$, indicating four low lying levels. At high temperature, the magnetic entropy attains the full theoretical value of $R \ln 9 =$ $18.27 \text{ J K}^{-1} \text{ mol}^{-1}$. The absence of a Schottky contribution to the heat capacity (inset of figure 6(b)) signals the fact that the ground state may be a fully degenerate J = 4 multiplet. Similar behaviour is observed in the PrSi system, in a recent report, where the Schottky contribution to the heat capacity is absent [18]. To understand the complex magnetic behaviour exhibited by PrGe, a detailed neutron diffraction study on the single crystal is necessary and is planned for the future.

5. Conclusion

Single crystals of PrGe were grown by the Czochralski pulling method in a tetra-arc furnace. X-ray analysis of the sample indicated the CrB-type structure as the only phase. The transport and the magnetic measurements clearly indicate that PrGe exhibits two magnetic orderings, at 44 K and 41.5 K, which are confirmed as antiferromagnetic and ferromagnetic, respectively. A strong anisotropy along the three principal crystallographic directions was observed, reflecting the orthorhombic symmetry of the crystal structure. The [001] direction was found to be the easy axis of magnetization, with a complete saturation of the Pr moment at about 0.4 T. The magnetization data measured at 1.8 K revealed hysteretic behaviour along all three directions, thus confirming the ferromagnetic nature of the configuration at this temperature. The absence of a Schottky contribution to the specific heat in the magnetic part of the heat capacity indicates a possible quasi-ninefold degenerate J = 4 ground state.

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